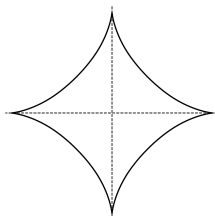


**PILOT LEARNING
CALCULUS II ENGINEERING
PROBLEM-SET 6
FALL 2019**

- (1) Find an equation of the tangent to the curve at the point corresponding to the given value of the parameter.
- (a) $x = t \cos t; y = t \sin t; t = \pi$
 - (b) $x = 1 + 4t - t^2; y = 2 - t^3; t = 1$
- (2) Find dy/dx and d^2y/dx^2 . For which values of t is the curve concave upward?
- (a) $x = t^2 + 1; y = e^t - 1$
 - (b) $x = 2 \sin t; y = 3 \cos t; 0 < t < 2\pi$
- (3) Find the points on the curve where the tangent is horizontal or vertical. You can check your work with a graphing software.
- (a) $x = e^{\sin \theta}; y = e^{\cos \theta}$
 - (b) $x = t^3 - 3t; y = t^2 - 3; 0 < t < 2\pi$
- (4) Consider the astroid

$$x = a \cos^3 \theta \quad y = a \sin^3 \theta$$



- (a) Find the slope of the tangent to the astroid in terms of θ .
 - (b) At what points is the tangent horizontal or vertical?
 - (c) At what points does the tangent have slope 1 or -1?
 - (d) Set up the integral to find the area of the region enclosed by the astroid.
- (5) Find the length of the following parametric curves.
- (a) $x = 1 + 3t^2; y = 4 + 2t^3; 0 \leq t \leq 1$
 - (b) $x = 3 \cos t - \cos 3t; y = 3 \sin t - \sin 3t; 0 \leq t \leq \pi$